COMPARING EXCHANGE RATE FORECASTABI L ITY: THE PARAGUAY CASE

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# COMPARING EXCHANGE RATE FORECASTABI L ITY: THE PARAGUAY CASE

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#### ABSTRACT

Forecasting exchange rates is a very difficult task. Since Meese and Rogoff's (1983) results showed that no model could outperform a driftless random walk in predicting exchange rates, there have been many papers which have tried to find some forecasting methodology that could beat the random walk, at least for certain forecasting periods. In particular, Wright (2008) introduced Bayesian Model Averaging as a tool to forecast exchange rates and Lam et al (2008) compared Bayesian Model Averaging and three structural models to a benchmark model (the random walk), both studies obtaining positive results. Also, Carriero et al (2009) found positive results using a Bayesian Vector Auto-regression model. The present paper is a small contribution to the same type of literature by comparing Purchasing Power Parity, Uncovered Interest Rate, Sticky Price, Bayesian Model Averaging, and Bayesian Vector Auto-regression models to the random walk benchmark in forecasting exchange rates between the Paraguayan Guarani and the US Dollar, the Brazilian Real and the Argentinian Peso. Forecasts are evaluated under the criteria of Root Mean Square Error, Direction of Change, and the Diebold-Mariano statistic. The results indicate that in shorter horizon forecasting BMA and BVAR can perform better but other models outperform the random walk at longer horizons.

#### 1 INTRODUCTION

Exchange rate forecasting is a complicated matter. It has been the subject of many studies which have yielded promising results only to be subsequently refuted by others. Attempts at formal exchange forecasting have existed for over a century. For instance, Purchasing Power Parity (PPP) was developed into a theory of exchange rate behavior already in the early twentieth century (Cassel, 1916). By the 1960s, it was the subject of "appraisals" (see literary review). In the same vein, Uncovered Interest Rate Parity (UIP) has been part of the discussion since the twenties (Keynes, 1923). Both of these models are still working horses in International Finance courses all over the world. The 1970s saw a burst of activity in exchange rate forecasting theory, with several models being developed one after the other - an activity which spilled into the early 1980s. And yet, a definitive model or framework remains elusive. The idea of efficient markets and the impossibility to predict asset prices consistently dates back to Fama (Fama, 1970) but, strangely, it took a few years before it made its way into international finance. In particular, since Meese and Rogoff (1983) argued that no model outperforms a driftless random-walk in forecasting exchange rates, researchers have been forced to go back to the drawing board to come up with more solid alternatives. For the following three decades, economists would go back and forth in arguing for and against the possibility of forecasting exchange rates. For instance, Lothian and Wu (2013) shows that Uncovered Interest Parity (UIP) has remarkable forecasting power in longer time horizons. But even recently, Cheung et al (2017) have reinforced the idea that no model can consistently beat a random walk.

The objective of the present work is to make a small contribution to the literature by expanding on the results obtained by Wright (2008) and extending the framework of Lam et al (2008). Both studies used Bayesian Model Averaging (BMA) to forecast the exchange rates of the U.S. Dollar (USD) with respect to several other currencies and then compare them to the performance of a benchmark model, namely, the driftless random walk. In particular, Lam et al also added three more structural models and compared them to the random walk as well. These models are the aforementioned PPP, and UIP and Sticky Price (SP). They are well-known models in the literature and have been extensively discussed, both in the past and in recent years. It is this latter approach that I have followed for this paper but I add one more model: a Bayesian Vector Auto-regression (BVAR) model with a Minnesota prior. As shown for instance by Carriero et al (2009), BVAR models perform well in the short run. I evaluate the performance of each model according to the Root Mean Square Error (RMSE) ratio, Direction of Change (DoC) ratio and the Diebold-Mariano (DM) statistic.

More specifically, I have used the above mentioned models to forecast the exchange rates between the Paraguayan Guarani (PYG) and the USD, the Brazilian Real (BRL) and the Argentinian Peso (ARS) using monthly data. Unlike Wright, I do not separate my variables into a financial and a macroeconomic data set in order to estimate monthly and quarterly exchange rates, respectively – all variables are monthly. Lam et al only produced forecasts based on quarterly data. The forecasting periods are 3, 6, 9, and 12 months ahead. The results are encouraging and in line with Wright's and Lothian and Wu's works, as well as Carriero et al: under the RMSE criterion, in the cases of the USD and BRL, BMA and BVAR outperform all other models in the 3-month and 6-month horizons; UIP outperforms all other models in the subsequent horizons; and, results are

similar under the DoC criterion. In the case of Argentina, PPP and SP appear to fare far better under both criteria, owing perhaps to Argentina's recent and complex history of inflation, and price and exchange rate volatility. Under the DM criterion, forecasts are statistically significant improvements in the 3-month horizon in the cases of BMA and BVAR for the PYG/USD, and only in the case of BVAR for PYG/BRL. UIP produces improved forecasts that are statistically significant only beyond 36 periods ahead for both exchange rates. As for the Argentinian peso, BVAR and SP forecasts are the statistically significant improvements over the random walk.

The rest of the paper proceeds as follows: in section 2, I discuss the previous literature related to exchange rate forecasting; in section 3, I describe the models and the reason for their choice; in section 4, I describe the data and their sources; in section 5, I present the results, briefly discussing them and I suggest possible further research; section 6 concludes.

#### 2 LITERATURE REVIEW

Exchange rate forecasting models have been around for over a hundred years now and the literature on forecasting theory and applications is extensive, to say the least. Models such as Purchasing Power Parity (PPP) and Uncovered Interest-Rate Parity (UIP) have been thoroughly analyzed time and again (see, for instance, Balassa (1964) for PPP and the aforementioned Lothian and Wu paper for UIP). Dornbusch (1976) proposed a Sticky Price (SP) model based on monetary fundamentals and Frankel (1979) further developed this framework by emphasizing the role of expectations. However, Meese and Rogoff (1983) wrote a seminal paper in which they argued that no exchange rate model can outperform a driftless random walk in out-of-sample forecasting. Since then, Mark (1995) proposed that at longer horizons a monetary fundamentals model could provide with better out-of-sample forecasts. This model has been subject to criticism by Killian (1999) and Faust et al (2003) where they argue that improvements occur only with a two-year window and disappear afterwards. Interestingly, Killian and Taylor (2003) finds that ESTAR models are helpful in explaining real exchange rate behavior. Also of interest to the present study is Barnett and Kwag's (2006) work which shows that the use of Divisia monetary aggregates and the User Cost Price dramatically improve the forecasting power of structural models. In a similar vein, Ghosh and Badhury (2018) show that Divisia Monetary aggregates are powerful indicators of exchange rate movements for several economies.

Authors have had some success in forecasting using large datasets as in Stock and Watson (2002) for the Index of Industrial Production, and Bernanke and Boivin (2003) for inflation. Moreover, Stock and Watson (2003) have used the combination of forecast methods to approximate output growth with encouraging results (the Bernanke and Boivin paper also utilizes forecast combination for inflation measures). It is worth noting that forecast combination methods can be dated back to Bates and Granger (1969).

Bayesian Model Averaging (BMA) was first introduced by Leamer (1978) and was further developed by Raftery et al (1997) and Hoeting et al (1999). BMA was first used for exchange rate forecasting by Wright (2008) and subsequently by Lam et al (2008). Both papers find that BMA produces improvements in out-of-sample forecasts when compared with a driftless random walk.

BVAR was used in forecasting as far back as Litterman (1986). Sarantis (2006) showed that a BVAR model outperforms a random walk in forecasting daily exchange rates.

Banbura et al (2007) used BVAR for forecasting employment, the Consumer Price Index (CPI) and the Fed Funds Rate with positive results for first-quarter predictions. Recently, Beckman et al (2018) have used VAR-based models with Bayesian estimation methods for exchange rate forecasting with some success.

#### 3 METHODOLOGY

In this section I will discuss the four different models that I have used to estimate the PYG/USD, PYG/BRL and PYG/ARS exchange rate forecasts and their respective specifications. In the choice of models I have followed Lam et al (2008) and, partly, Cheung et al (2017). I will also explain how I have evaluated the performance of each model.

#### 3.1 Purchasing Power Parity

PPP is well-known and – as mentioned in the previous section – widely discussed theoretical model which gives a clear and intuitive explanation for exchange rate determination. The PPP model is expressed in the following manner:

$$ln e_t = ln p_t - ln p_t^* \tag{1}$$

where  $e_t$  is the nominal exchange rate,  $p_t$  is the domestic price and  $p_t^*$  is the foreign price. These are, of course, price indexes and not price levels.

The PPP specification I use here follows Lam et al (2008). This involves an errorcorrection restriction and no short-run dynamics. What this means is that the variation from the exchange rate is a correction of the deviation from a long-run equilibrium in the previous period. The form of the equation is then

$$\ln e_{t+h} - \ln e_t = \alpha_0 + \alpha_1 (\ln e_t - \beta_0 - \beta_1 \ln \tilde{p}_t) + \epsilon_t \tag{2}$$

where  $\tilde{p}_t$  is the relative price level of the domestic economy relative to the foreign one, h is the forecast horizon and  $\epsilon_t$  is the error term.

#### 3.2 Uncovered Interest-rate Parity

UIP is another model that has been studied repeatedly as an approximation to forecasting exchange rates. This model entails the no-arbitrage condition that the expected return of the exchange rate h periods ahead is equal to the interest rate differential, which can be expressed thus:

$$E_t(\ln e_{t+h} - \ln e_t) = i_t - i_t^* \tag{3}$$

where  $E_t$  is the expectation and  $i_t$  and  $i_t^*$  are the domestic and foreign interest rates, respectively.

In a similar specification as the one above for the PPP model, also including an errorcorrection restriction, we write the equation as

$$\ln e_{t+h} - \ln e_t = \alpha_0 + \alpha_1 (\ln e_t - \beta_0 - \beta_1 \ln \tilde{i}_t) + \epsilon_t \tag{4}$$

Here the  $\tilde{i}_t$  is the relative interest rate (domestic to foreign).

#### 3.3 Sticky Price

For this model we follow Frankel (1979) and expand the PPP framework so that exchange rates now are also determined by money supply, output and interest rates. This is given by the equation

$$\ln e_t = \ln m_t - \ln m_t^* - \phi(\ln y_t - \ln y_t^*) + \lambda(\ln i_t - \ln i_t^*) + \beta(\ln \pi_t - \ln \pi_t^*)$$
 (5)

where  $m_t$  and  $m_t^*$ ,  $y_t$  and  $y_t^*$ ,  $i_t$  and  $i_t^*$ , and  $\pi_t$  and  $\pi_t^*$  are, respectively, domestic and foreign money supply, domestic and foreign output, domestic and foreign interest rates and domestic and foreign current long-run expected rates of inflation.

As in the above cases, we use a restrictive error correction form of the model:

$$\ln e_{t+h} - \ln e_t = \alpha_0 + \alpha_1 (\ln e_t - \beta_0 - \beta_1 \ln \tilde{m}_t - \beta_2 \ln \tilde{y}_t - \beta_3 \ln \tilde{i}_t - \beta_4 \ln \tilde{p}_t) + \epsilon_t$$
 (6)

Here  $\tilde{m_t}$ ,  $\tilde{y_t}$ , and  $\tilde{i_t}$  are domestic to foreign relative money demand, output and short-term interest rates, respectively. Notice that we have replaced long-run expected rates of inflation with the only proxy available - relative prices. The reason for this choice will be explained in the next section.

#### 3.4 Bayesian Model Averaging

BMA is a forecasting method that utilizes large datasets and many different models. Say there are  $M_i$  models, i=1,...n each of which has a parameter  $\theta_i$ . One does not know which model is the true model but assumes that one of them is. One assumes the *ith* model is the true model based on some prior belief  $P(M_i)$ . Posterior probabilities are computed starting from a prior about which model is the true one. So if D is the data, we have

$$P(M_i|D) = P(D|M_i)P(M_i) / \sum_{j=1}^{n} P(D|M_j)P(M_j)$$
 (7)

where

$$P(D|M_i) = \int P(D|\theta_i, M_i) P(\theta_i|M_i) d\theta_i$$
 (8)

Here  $M_i$ 's marginal likelihood is  $P(D|M_i)$ ,  $P(\theta_i|M_i)$  is the prior density of the parameters and the likelihood is given by  $P(D|\theta_i, M_i)$ . The forecasts from each of the different models are then weighted by their respective posteriors. The model is assumed to be linear. And so, one has

$$y = X_i \beta_i + \epsilon \tag{9}$$

where y is the vector of exchange rates (in this case),  $X_i$  are the predictors,  $\beta_i$  are parameters and  $\epsilon$  is the mean zero, i.i.d. error with variance  $\sigma^2$  and  $\theta_i = (\beta_i', \sigma^2)$ . Strict exogeneity is assumed of all regressors. As for the coefficients, I assume a prior mean of zero. The structure of their variance is given by Zellner's g so that

$$B_i|g\ N(0,\sigma^2(1/gX_i'X_i)^{-1})\tag{10}$$

where the hyperparameter g is set to the default "unit information prior" g=n (the number of models).

The forecasting model is then given by

$$\ln e_{t+h} - \ln e_t = \beta_i' X_{i,t} + \epsilon_t \tag{11}$$

where  $X_{i,t}$  is the vector of regressors at time t for model i. For each model I have a forecast  $\tilde{\beta}'_i X_{i,t}$  where  $\tilde{\beta}'_i$  is the posterior mean of  $\beta_i$ . Each model is weighted by their posterior probabilities so that the forecast is given by  $\sum_{i=1}^n P(M_i|D)\tilde{\beta}'_i X_{i,t}$  where  $P(M_i|D)$  is the posterior probability of the ith model and D is the dataset. Following Wright (2008) and Lam et al (2008) I consider the following variables as potential predictors from a monthly dataset: (i) short-term interest rates and relative short-term interest rates, (ii) log of output and log of relative output (domestic to foreign), (iii) log of money supply and log of relative money supply (domestic to foreign), (iv) log of price levels and log of relative price levels (domestic to foreign), (v) oil price, and for the particular case of Paraguay, (vi) soy price. This gives a total of  $2^6$  possible models.

## 3.5 Bayesian Vector Auto-regression

The BVAR model with a Minnesota prior was introduced in the aforementioned paper by Litterman and, as previously described, has been widely used in forecasting. If the model is as follows

$$y = (I_m \otimes X)\alpha + \epsilon, \epsilon \sim (0, \Sigma_{\epsilon} \otimes I_T)$$
(12)

then y and  $\epsilon$  are  $mT \times 1$  vectors of dependent variables and errors, respectively, and where m is the number of variables and T, the time periods.  $I_m$  is the identity matrix, X is the matrix of independent variables and  $\alpha$  is a  $ml \times 1$  vector where l is the number of lags. More specifically,  $\alpha = \bar{\alpha} + \xi_{\alpha}$  with  $\xi_{\alpha} \sim N(0, \Sigma_{\alpha})$ , where in the Minnesota prior  $\bar{\alpha} = 0$  except  $\bar{\alpha}_{1i} = 1, i = 1, ..., m$ ,  $\Sigma_{\alpha}$  is diagonal and each element  $\sigma_{ij,l}$  (equation i, variable j, and lag l) is as follows

$$\sigma_{ij,l} = \phi_0/h(l), i = j \tag{13}$$

If j is endogenous, then

$$\sigma_{ij,l} = \phi_0 \times \phi_1 / h(l) \times (\sigma_j / \sigma_i)^2, i \neq j$$
(14)

And if j is exogenous, then

$$\sigma_{ij,l} = \phi_0 \times \phi_2 \tag{15}$$

In this case  $\phi_0, \phi_1, \phi_2, (\sigma_j/\sigma_i)^2$  and h(l) are, respectively, hyperparameters, a scaling factor, and a function of lags l. Note that  $\phi_0$  measures the tightness of the first lag's variance,  $\phi_1$  is the relative tightness of any other variables, and  $\phi_2$  is the relative tightness of exogenous variables. Finally, h(l) is a measure of the relative tightness of the variance of the lags.

The error correction model follows a similar process to the one laid out for the SP model, using the same variables. The number of lags is 1.

# 3.6 Out-of-Sample Performance Evaluation: Root Mean Square Error Ratio and Direction of Change

In this paper I use what is called in the literature a rolling regression in order to produce the predicted forecasts. I first pick an in-sample period for which the models are first estimated and then exchange rates are forecasted for the out-of-sample period. The sample is then updated to the following period until there are no more out-sample-sample observations.

In order to evaluate how well each model is performing I have compared each one to a benchmark model which in this case is the driftless random-walk given by

$$\ln e_{t+h} - \ln e_t = \epsilon_t \tag{16}$$

Following Meese and Rogoff's methodology, I take the expectation of the random walk so that it becomes a martingale process, i.e. the predictor of the exchange rate h periods ahead is whatever the exchange rate is at time t.

First, I use the root mean square error (RMSE) of each of the four models and divide it by the RMSE of the random-walk. A ratio of less than one indicates that the model is performing better than the random-walk and viceversa. I asses the out-of-sample performance of each model 3, 6, 9 and 12 months ahead.

The second method of evaluation is the Direction of Change (DoC) ratio where I measure the proportion of times each model correctly predicts whether the actual exchange rate increases or decreases. Assuming that the expected value of random walk predicting the right DoC is 0.5, values above 0.5 indicate that a model is outperforming the random walk. The higher the proportion is, the better the model is performing.

The third method is the statistic produced by Diebold & Mariano (1995), which allows for the comparison of forecasts in terms of whether the difference between two forecasts for the same forecasting period is statistically significant and whether the improvement is statistically significant (and thus, one forecast is "better" than another). If  $g(e_{it})$  is the loss function of a forecast error, the loss differential function is defined as  $d_t = g(e_{1t}) - g(e_{2t})$ . If  $d_t$  is zero, then the forecasts under examination are equally accurate. Under the null, the expected value of  $d_t$  is zero. The DM statistic itself takes the form

$$DM = \bar{d}/\sqrt{2\pi \hat{f}_{d(0)}/T} \tag{17}$$

where  $\bar{d}$  is the sample mean of the loss differential function and  $\hat{f}_{d(0)}$  is a consistent estimate of the spectral density. Under the null,  $DM \to N(0,1)$ . The null is rejected if  $|DM| > z_{\alpha/2}$ .

#### 4 data

The data for this study are monthly series of the above mentioned variables starting in January, 1994 up to July, 2017 for the PYG/USD exchange rate; January, 1994 to December, 2016 for Brazil; and, January, 1997 to December, 2016 for Argentina. The reason I chose to start the series at these particular dates is that before January 1994 there were scarce to none monthly Paraguayan data available and in the case of Argentina, because there was no monthly exchange rate data available prior to 1997. The choice of

in-sample and out-of-sample data was done based on the conclusion of the Paraguayan Stand-by agreement with the International Monetary Fund (IMF) in 2004 regarding the payment of its foreign debt. Therefore, the out-of-sample prediction period starts in January 2005.

The choice of short-term interest rates for the SP model was done not only following Frankel's methodology but also out of necessity: it is the only interest rate that has been consistently reported since 1994. We should also point out that these are interest rates on the bonds that the Central Bank of Paraguay (BCP) trades with Paraguayan private banks as a monetary policy tool. For the same reason, they are the interest rates used in the UIP model. On a similar note, the choice of Consumer Price Index (CPI) as a proxy for expected inflation was also done following Frankel and out of necessity: of all the possible proxies used by Frankel, it was the only one available. The proxy for monthly Paraguayan, Argentinian and Brazilian GDP were, respectively: the Monthly Economic Activity Index (IMAEP) produced by the BCP which tracks the performance of the most relevant Paraguayan industries; the Monthly Estimator of Economic Activity (EMAE) produced by the National Institute of Statistics and Census (INDEC) in Argentina; and, the Index of Monthly Monetary Activity (IBC-Br) produced by the Central Bank of Brazil (BCB). Finally, soy prices were included in the BMA model because they are the main Paraguayan export and they represent a significant portion of Argentinean and Brazilian exports as well. Also, the soy market is highly dolarized.

All the data pertaining to Paraguay, as well as oil and soy prices, were obtained from the Statistical Annex of the yearly Economic Report published by the BCP. M1 monetary aggregates, CPI and three-month Treasury bill interest rates for the US were retrieved from the Federal Reserve Bank of Saint Louis' Federal Reserve Economic Data (FRED). As for US monthly GDP data, they were obtained from the Macroeconomic Advisers data bank. The Brazilian data were taken from the BCB statistical bulletin, except the CPI which was retrieved from the Getulio Vargas Foundation site.

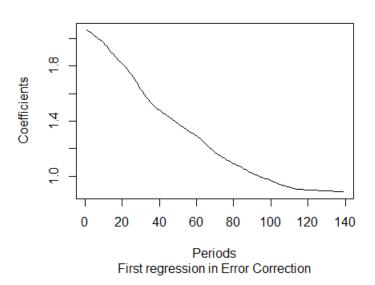
Argentinian data merit an observation. Their M1 aggregates were taken from the FRED, and interest rates, from the Central Bank of the Argentine Republic's (BCRA) site. But the CPI had to be constructed from four different sources: the original CPI series from INDEC (base year 2008), a second CPI series from INDEC (base year 2014), a third CPI series from INDEC (base year 2016) and a parallel series put together by the Argentine Congress, as the INDEC stopped producing its CPI series from November, 2015 to November, 2016. This series was retrieved from *Ambito.com*, the internet site which compiled it.

#### 5 RESULTS

#### 5.1 Coefficients in the PPP and UIP models

Before discussing the results themselves, below are graphs depicting the behavior of the coefficients for the PPP and UIP models in the first regression of the error correction. As might be expected, they almost always differ from 1. The PPP coefficients for the PYG/USD exchange rate follow a neat downward trajectory ranging from 2.06 in the first period to 0.885 at its lowest in the last period. The coefficients for the PYG/BRL and PYG/ARS range from a low of -0.25 (in the first period) to a high of -0.13 (November,

#### PPP PYG/USD



2013) and from 1.22 (in the first period) to a high of 3.24 (September, 2015). The graphs also show that the latter two exchange rate coefficients behave somewhat similarly but differ greatly from the PYG/USD coefficients.

UIP coefficients for the PYG/USD exchange rate vary from a low of 0.039 (September, 2007) to a high of 0.17 in the first period. The PYG/BRL coefficients range from -0.022 (November, 2009) to 0.095 (March, 2007). As for the PYG/ARS coefficients, they hit a low of 0.163 (December, 2005) and high of 0.316 in the last period.

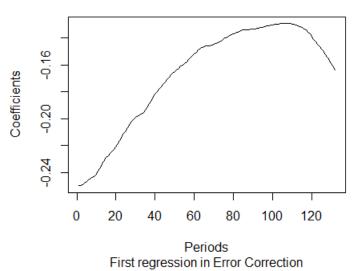
What all of this does is to underscore the need to adjust the models by using an error-correcting approach, as these relations are clearly not stable across time and can vary greatly from model to model and from case to case.

#### 5.2 Comparing Models using RMSE

As discussed in section 3, we are using the ratio of the RMSE of each model to the RMSE of the random-walk in order to asses their performance (recall that a ration of less than 1 is an improvement over the random walk, and vice-versa). Tables 1, 2 and 3 show the RMSE ratios of the PYG/USD, PYG/ARS and the PYG/BRL, respectively. In tables 1 and 3 (US and Brazil) we can see that BMA and BVAR outperform all other models in the 3-month and 6-month forecasting horizons and UIP outperforms all other models in the following forecasting horizons. PPP appears to also do well in longer forecasting horizons.

In the case of PYG/ARS, results are quite different. PPP and SP outperform UIP and BMA, but BVAR in particular does exceedingly well. UIP, on the other hand, does not do better than the random walk in any of the forecasting horizons, in contrast with what is observed in tables 1 and 3. As we will see in the following subsections, this pattern will keep repeating itself.





# PPP PYG/ARS

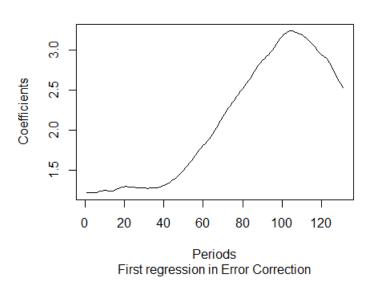
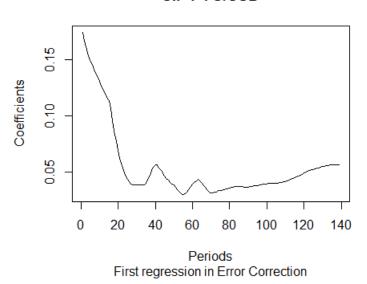


Table 1: Ratio of Model's RMSE over Random Walk RMSE

	3 months	6 months	9 months	12 months
PPP	0.99386	1.02949	1.08196	1.15853
UIP	1.00108	0.98777	0.97286	0.95796
SP	1.04635	1.10185	1.16113	1.24188
BMA	0.88046	0.96462	1.02745	1.03807
BVAR	0.84261	0.97718	1.06516	1.12876





# **UIP PYG/BRL**

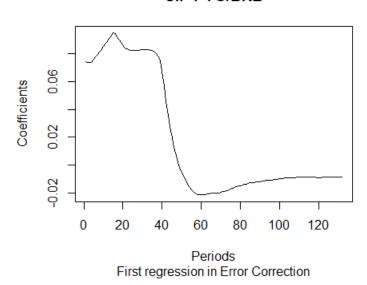
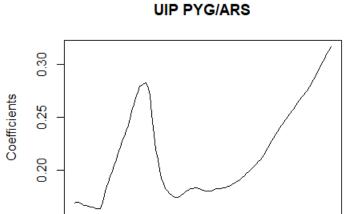


Table 2: Ratio of Model's RMSE over Random Walk RMSE

	3 months	6 months	9 months	12 months
PPP	0.95493	0.96508	0.95008	0.87946
UIP	1.00936	1.15046	1.20009	1.16285
SP	0.99463	0.91584	0.85797	0.81159
BMA	1.06341	0.96848	0.94650	0.93006
BVAR	0.73696	0.83135	0.81192	0.78303



Periods
First regression in Error Correction

Table 3: Ratio of Model's RMSE over Random Walk RMSE

	3 months	6 months	9 months	12 months
PPP	1.01075	1.00422	0.99794	0.99295
UIP	1.00860	1.00017	0.99258	0.98710
SP	1.09976	1.17235	1.25832	1.39325
BMA	0.93393	0.99465	1.03617	1.01704
BVAR	0.79494	0.95689	1.04981	1.11189

### 5.3 Comparing Models using DoC

Tables 4, 5 and 6 show the ratios of DoC for the PYG/USD, PYG/ARS and PYG/BRL, respectively. There are two ways in which we can analyze results under this criterion. Assuming, as previously mentioned, that a random walk will correctly predict the direction of change half the time (an expected value of 0.5), then all models outperform it in the first and last forecasting horizons in table 4 (except BVAR in the last period), with BMA having the largest ratio in the 3-month period and SP, in the 12-month period. In table 5, all models outperform the random walk in all forecasting periods, especially in the 12-month horizon where UIP and PPP give the highest proportions. In table 6, all models beat the random walk in the first period, but only BMA and BVAR outperform it in the second period, only BVAR in the third period, and in the fourth forecasting period, SP produces the highest proportion.

Notice though that if the actual random walk forecasts are taken as as reference, what the results say changes. Using this metric, in table 4 BMA and BVAR outperform all models in the first two forecasting horizons, BVAR and PPP in the third and all except BVAR do better in the 12-month horizon. In table 5 only PPP outperforms the random walk in the first three forecasting horizons, and BVAR, in the first and third horizons, and none in the last horizon. In table 6, in the first forecasting horizon BMA and PPP outperform the random walk; in the second, all except SP; in the third, SP and BVAR; and in the fourth, UIP, SP, and BMA.

It is clear, of course, that if enough iterations of the experiment were made, the random walk would tend to its expected value of 0.5 but it is nonetheless interesting to make both comparisons, as they give slightly different interpretations. If we do not constantly repeat the very same experiment, the realized values of the random walk do not exactly behave as a random walk.

3 months	6 months	9 months	12 months
0.51471	0.42857	0.47692	0.52756
0.51471	0.43609	0.49231	0.53543
0.51471	0.42857	0.46154	0.53543
0.52206	0.42857	0.46923	0.55906
0.56618	0.48120	0.44615	0.50394
0.55147	0.48120	0.54615	0.46457
	0.51471 0.51471 0.51471 0.52206 0.56618	0.51471       0.42857         0.51471       0.43609         0.51471       0.42857         0.52206       0.42857         0.56618       0.48120	0.51471       0.42857       0.47692         0.51471       0.43609       0.49231         0.51471       0.42857       0.46154         0.52206       0.42857       0.46923         0.56618       0.48120       0.44615

Table 4: Ratio of Direction of Change

#### 5.4 Comparing models using the DM statistic

In order to see if the forecasts produced by some of the models are statistically significantly different and better than those produced by the random walk, these forecasts are compared using the DM statistic. PPP and SP statistics for the PYG/USD and PYG/BRL are not present as they do not improve on random walk forecasts. In the case of the PYG/ARS exchange rate, all models and their corresponding tables are below as

	3 months	6 months	9 months	12 months
RW	0.54688	0.54400	0.52459	0.61345
PPP	0.55469	0.56000	0.54918	0.61345
UIP	0.56250	0.56800	0.51639	0.60504
SP	0.53125	0.57600	0.50000	0.60504
BMA	0.55469	0.53600	0.50820	0.54622
BVAR	0.57812	0.52800	0.54918	0.55462

Table 5: Ratio of Direction of Change

Table 6: Ratio of Direction of Change

	3 months	6 months	9 months	12 months
RW	0.53488	0.42857	0.44715	0.48333
PPP	0.54264	0.44444	0.43902	0.47500
UIP	0.53488	0.43651	0.43902	0.49167
SP	0.51938	0.42857	0.46341	0.55000
BMA	0.56589	0.50794	0.42276	0.50833
BVAR	0.52713	0.53175	0.51220	0.43333

the behavior differs greatly from that of the first two exchange rates. Also, the forecasting periods for UIP now reach up to 48 months so as to show that as forecasting horizons become larger, forecasts produced by UIP are statistically significant improvements on the random walk.

In the long run, tables 7 and 10 show that by the 48th forecasting horizon, UIP forecasts are statistically significant improvements over the random walk forecasts at the 1% level for both the PYG/USD and PYG/BRL forecasts. In the three month horizon, BMA and BVAR produce forecasts that also improve on the random walk and are statistically significant at the 5% level for the PYG/USD exchange rate (Tables 8 and 9). In this same horizon, BMA does not produce a statistically significant improvement for the PYG/BRL exchange rate but BVAR does at the 1% level (Tables 11 and 12).

Tables 13 through 17 show the DM statistics and p-values for the PYG/ARS exchange rate. They are the opposite of the results in the previous tables. Although PPP again does not do any better than random walk forecasts, UIP produces no improvement either (Tables 13 and 14). Instead, it is the SP model that produces the statistically significant improvements in the longer horizons (Table 15). BMA does not work well in the short run but BVAR does, both in the short run and the long run (Tables 16 and 17).

#### 5.5 Discussion

The above results are encouraging but also puzzling. The performance of BMA is consistent with Wright's findings in that BMA's forecasting power diminishes in longer forecasting horizons but can outperform the random-walk in the 3 and 6-month periods. This is

Table 7: Diebold-Mariano Statistic UIP PYG/USD

	DM UIP	p-value UIP
3 months	0.39654	0.65410
6 months	0.02622	0.51050
9 months	-0.24012	0.40510
12 months	-0.41955	0.33740
24 months	-0.90075	0.18390
36 months	-1.03720	0.14980
48 months	-4.40530	0.00001

Table 8: Diebold-Mariano Statistic BMA PYG/USD

	DM BMA	p-value BMA
3 months	-1.69310	0.04522
6 months	-1.15690	0.12370
9 months	0.24600	0.59720
12 months	0.38388	0.64950

Table 9: Diebold-Mariano Statistic BVAR PYG/USD

	DM BVAR	p-value BVAR
3 months	-1.73600	0.04128
6 months	0.03673	0.51460
9 months	0.97573	0.83540
12 months	1.16230	0.87740

Table 10: Diebold-Mariano Statistic UIP PYG/BRL

	DM UIP	p-value UIP
3 months	0.80299	0.78900
6 months	0.40647	0.65780
9 months	0.20580	0.58150
12 months	0.09330	0.53720
24 months	-0.80289	0.21100
36 months	-0.92069	0.17860
48 months	-3.93600	0.00004

Table 11: Diebold-Mariano Statistic BMA PYG/BRL

	DM BMA	p-value BMA
3 months	-0.79202	0.21420
6 months	-0.26083	0.39710
9 months	0.18570	0.57370
12 months	-0.03754	0.48500

Table 12: Diebold-Mariano Statistic BVAR PYG/BRL

	DM BVAR	p-value BVAR
3 months	-2.33640	0.00973
6 months	-0.42412	0.33570
9 months	0.85064	0.80250
12 months	1.06440	0.85640

Table 13: Diebold-Mariano Statistic UIP PYG/ARS

	DM UIP	p-value UIP
3 months	1.85080	0.96790
6 months	0.96790	0.97270
9 months	1.68280	0.95380
12 months	1.43750	0.92470

Table 14: Diebold-Mariano Statistic PPP PYG/ARS

	DM PPP	p-value PPP
3 months	-0.11886	0.45270
6 months	1.06470	0.85650
9 months	0.89264	0.81400
12 months	0.24573	0.59710

Table 15: Diebold-Mariano Statistic SP PYG/ARS

	DM SP	p-value SP
3 months	-0.10973	0.45630
6 months	-1.64470	0.05002
9 months	-4.19740	0.00001
12 months	-7.22450	0

Table 16: Diebold-Mariano Statistic BMA PYG/ARS

-		
	DM BMA	p-value BMA
3 months	2.05080	0.97990
6 months	0.95237	0.82950
9 months	0.74075	0.77060
12 months	0.46682	0.67970

Table 17: Diebold-Mariano Statistic BVAR PYG/ARS

-		
	DM BVAR	p-value BVAR
3 months	-2.66800	0.00382
6 months	-2.91120	0.00180
9 months	-4.22160	0.00001
12 months	-5.43310	0.0000000

particularly true in this study of the PYG/USD and PYG/BRL exchange rates, whose forecasts seem to behave similarly. This is also true of the forecasts produced by BVAR which in the short-run perform better than those produced by BMA, except at the 6-month horizon in the case of the PYG/USD exchange rate.

If we consider Lothian and Wu's findings that UIP performs well in longer time horizons, it is consistent that UIP outperforms all models in 9-month and/or 12 month-ahead periods (under RMSE) and beyond (where the improvement actually becomes statistically significant) in the US and Brazil case. These results are mostly congruent using the three evaluation criteria if under DoC the reference is the actual forecast produced by the random walk and not its assumed expected value. In the latter case, results are much less informative.

The case of Argentina is different and somewhat puzzling. Under the RMSE criterion, BMA and BVAR forecasting power gets better, not worse, in longer time horizons, and UIP never outperforms the random walk. However, under DoC and comparing actual forecasts BMA and BVAR forecasts improve on the random walk in the 3 month horizon, as expected. Here, again, UIP does not outperform random walk in the longer run. This is in direct contrast with the above-discussed results. One explanation may be that Argentina had a contentious history with inflation during the period under study and its monetary and fiscal policies were rather volatile. So much so that publications such as *The Economist* refused to publish governmental data on inflation because it was considered highly innacurate <sup>1</sup> (eventually, as mentioned earlier, even the government stopped publishing its own CPI for a year). It is perhaps because of this that the model that focuses on prices and the monetary aggregates do better in forecasting exchange rates: it is what economic agents payed most attention to when dealing with the Argentinian Peso. Finally, the DM criterion evaluation is largely consistent with the RMSE criterion. UIP forecasts' improvement

<sup>1</sup> see for instance The Economist. Don't lie to me, Argentina at https://www.economist.com/node/21548242

becomes statistically significant in the long-run and most of the short-run improvements produced by BMA and BVAR are also statistically significant. Something that calls the attention is that BVAR p-values become more and more statistically as the forecasting horizon is extended. This is the opposite of what we see in the case of the other exchange rate forecasts. Perhaps this owes something to faulty data produced by Argentina in the period under discussion.

#### 5.6 Further Research

The present study could be expanded in different directions. First, the same models could be used to forecast the behavior of the PYG exchange rate with respect to other relevant currencies.

Another avenue of research could be the inclusion of other forecasting models and compare their performances to the benchmark model. Some posibilities include GARCH models (see for instance Pilbeam and Langeland (2014)) or Copula models (see Cerrato et al (2015)).

A perhaps more laborious possibility could involve the calculation of Divisia Monetary Aggregates for Paraguay and then include them in the pertinent models. Barnett and Kwag (2006) have already used these aggregates in the several structural models to forecast the exchange rate between the US Dollar and the British Pound. A similar experiment would be to include Divisia monetary aggregates in the Bayesian models to verify if they have a greater weight in forecasting exchange rates or if they can help in their improvement.

#### 6 CONCLUSION

The academic discussion on exchange rate forecasting has existed for over a century. In all this time, the arguments for and against the possibility of actually being able to produce significant forecasts has gone back and forth, and the strength of either argument hast ebbed and flowed, depending on the context. The conventional wisdom in the profession seems to be anchored in the idea that markets are indeed efficient and that a consistent method of forecasting does not exist. In that sense, the present study "goes agains the grain," as it were, in arguing that we can contribute to finding the elusive forecasting methodology that will fit different contexts.

Even if improvements are only contextual, these methods can still be relevant for policy. For the Paraguayan economy, exchange rates are a very important matter. Its main exports are traded in a highly dolarized market. As a small, open economy, Paraguay also imports a number of goods traded in dollars, among them, of course, oil. Paraguay's largest neighbors and trading partners are Argentina and Brazil, and these exchange rates are indeed relevant. Therefore, the ability to forecast the PYG/USD, PYG/ARS and PYG/BRL exchange rates would be a powerful tool for both monetary and fiscal policy. In that spirit, it has been the objective of this paper to compare and assess the performance of five different models of exchange rate determination: PPP, UIP, SP, BMA and BVAR. In order to do so, we have used as criteria the RMSE and DoC ratios and the DM statistic.

The obtained results seem to indicate that, in the case of PYG/USD and PYG/BRL, UIP, BMA and BVAR forecasts improve on all other models, although neither produces the

best forecast for every period: BMA and BVAR have more power in the shorter forecasting horizons and UIP in the longer ones. This is in line with previous studies, in particular Wright (2008) and Lothian and Wu (2011). Argentina's case is different but this may have to do with its recent economic history or faulty data, or both. Further research could shed more light on the forecastability of exchange rates in the different parts of the world.

# 7 APPRENDIX: MSE TABLES

The following are are the Mean Square Error tables for the PYG/USD, PYG/ARS and PYG/BRL, respectively.

Table 18: Root Mean Square Error of each Model

	3 months	6 months	9 months	12 months
PPP	0.00352	0.00905	0.01435	0.01967
UIP	0.00357	0.00833	0.01161	0.01345
$\operatorname{SP}$	0.00390	0.01037	0.01653	0.02260
BMA	0.00276	0.00794	0.01294	0.01579
BVAR	0.00253	0.00815	0.01391	0.01867
Random Walk	0.00356	0.00854	0.01226	0.01466

Table 19: Root Mean Square Error of each Model

	3 months	6 months	9 months	12 months
PPP	0.00690	0.01716	0.02846	0.03465
UIP	0.00771	0.02438	0.04541	0.06058
$\operatorname{SP}$	0.00748	0.01545	0.02321	0.02951
BMA	0.00855	0.01728	0.02825	0.03875
BVAR	0.00411	0.01273	0.02078	0.02747
Random Walk	0.00756	0.01842	0.03153	0.04480

Table 20: Root Mean Square Error of each Model

	3 months	6 months	9 months	12 months
PPP	0.00367	0.00870	0.01238	0.01483
UIP	0.00366	0.00863	0.01225	0.01466
$\operatorname{SP}$	0.00435	0.01185	0.01969	0.02920
BMA	0.00314	0.00853	0.01335	0.01556
BVAR	0.00227	0.00790	0.01370	0.01860
Random Walk	0.00360	0.00862	0.01243	0.01504

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#### REFERENCES

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